

CASE EXAMPLE

| s | $p(s)$ | $r(s)$ |
|-----|--------|--------|
| 1 | .2 | -.05 |
| 2 | .2 | .1 |
| 3 | .6 | .2 |

$$r_f = .05$$

$$r_{\text{prime}} = .07$$

$$1. \quad E(r_p) = \sum_{s=1}^3 p(s)r(s)$$

$$= p(1)r(1) + p(2)r(2) + p(3)r(3)$$

$$= .2(-.05) + .2(.1) + .6(.2)$$

$$= .13$$

$$\boxed{E(r_p) = 13\%}$$

$$\sigma_p^2 = \sum_{i=1}^3 p(i)[r(i) - E(r_p)]^2$$

$$= .2(-.18)^2 + .2(-.03)^2 + .6(.07)^2$$

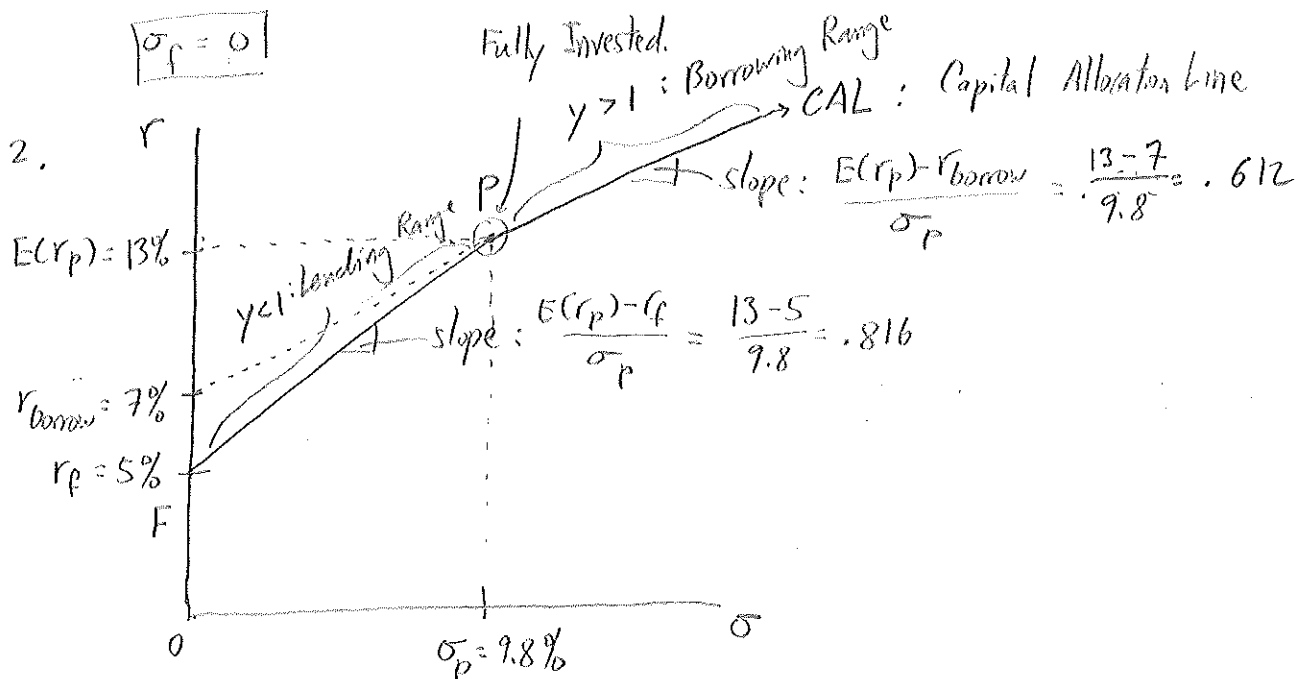
$$= .0096$$

$$\sigma_p = .09798$$

$$\boxed{\sigma_p = 9.80\%}$$

$$\boxed{r_f = 5\%}$$

$$\boxed{\sigma_f = 0}$$



3. $y = .75$

$$E(r_c) = r_f + y [E(r_p) - r_f]$$
$$= 5\% + .75(13\% - 5\%)$$

$$\boxed{E(r_c) = 11\%}$$

$$\sigma_c = y \sigma_p$$
$$= .75(9.8\%)$$

$$\boxed{\sigma_c = 7.35\%}$$

4. $y = 1.25$

$$E(r_c) = r_{\text{borrow}} + y [E(r_p) - r_{\text{borrow}}]$$
$$= 7\% + 1.25(13\% - 7\%)$$

$$\boxed{E(r_c) = 14.5\%}$$

$$\sigma_c = y \sigma_p$$
$$= 1.25(9.8\%)$$

$$\boxed{\sigma_c = 12.25\%}$$

5. If I NEED 12% return on average, then:

$$12\% = r_f + y [E(r_p) - r_f]$$
$$= 5\% + y(8\%)$$

$$y = \frac{7}{8}$$

$$y = .875$$

Thus, allocate 87.5% of assets, or \$144,375 into the risky assets.

$$\sigma_c = y \sigma_p$$
$$= .875(9.8\%)$$

$$\boxed{\sigma_c = 8.575\%}$$

Thus, with 95% certainty, the returns to this portfolio lie between a \$8,497.5 loss and \$48,097.5 gain.

$$6. \quad \sigma_c = 8\%$$

$$\sigma_c = \gamma \sigma_p$$

$$= \gamma (9.8\%)$$

$$\gamma = \frac{8}{9.8}$$

$$\gamma = 0.816327$$

Thus, allocate 81.63% of funds into risky assets.

$$E(r_c) = r_f + \gamma [E(r_p) - r_f]$$

$$= 5\% + 0.816327 (8\%)$$

$$\boxed{E(r_c) = 11.53\%}$$